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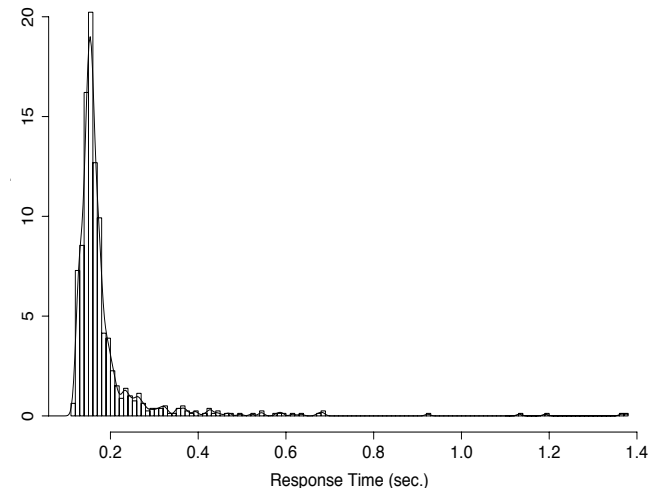
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# Heavy-tailed Distribution of Parallel I/O System Response Time

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# Outline

- Motivation
- Response time sampling method
- Analysis results of response time

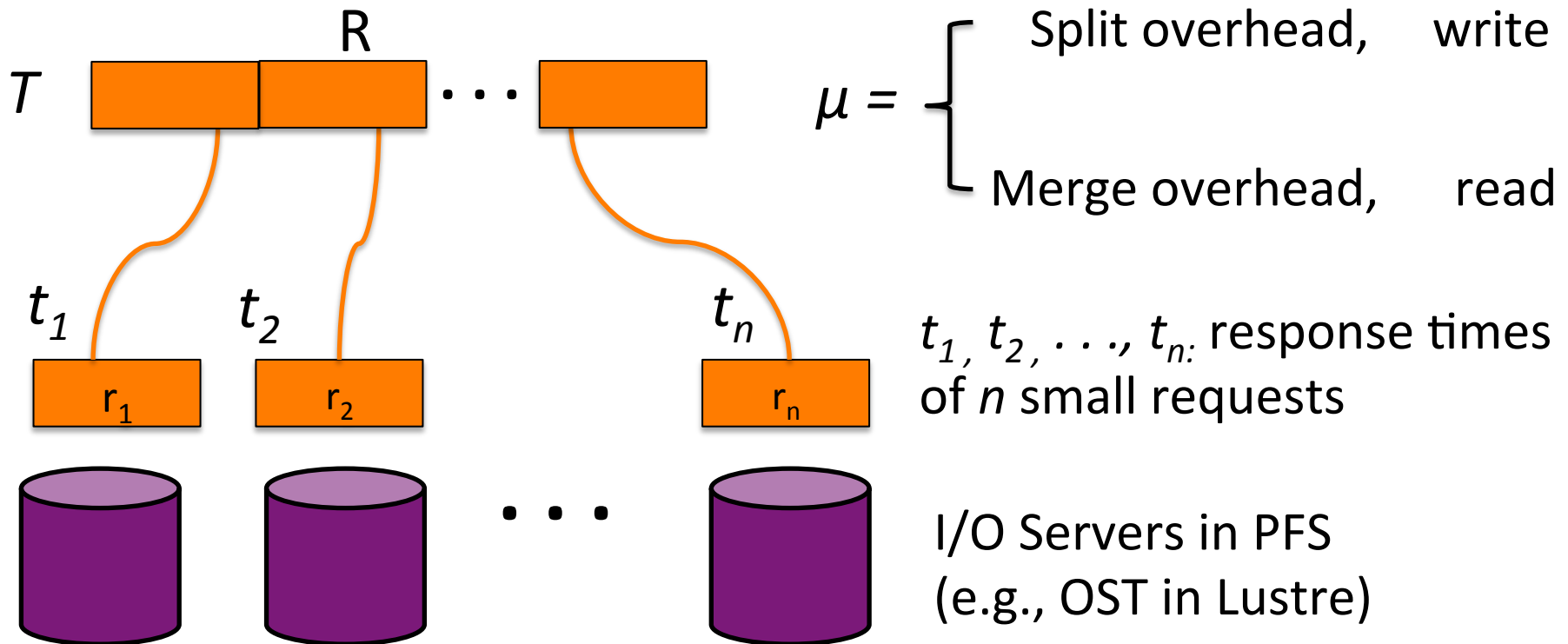
# Estimating Response Time of I/O is Essential Element

- Data analysis query plan optimizing
  - Choose index or data organization with minimum read time
  - Scientific Data Services (SDS) framework, PostgreSQL, SciDB
- Data writing performance tuning
  - Select striping size, striping account, and other parameters to reduce write time
  - ExaHDF5, I/O Scheduler
- Simulator, Job Scheduler , Quality of service (QoS), etc.

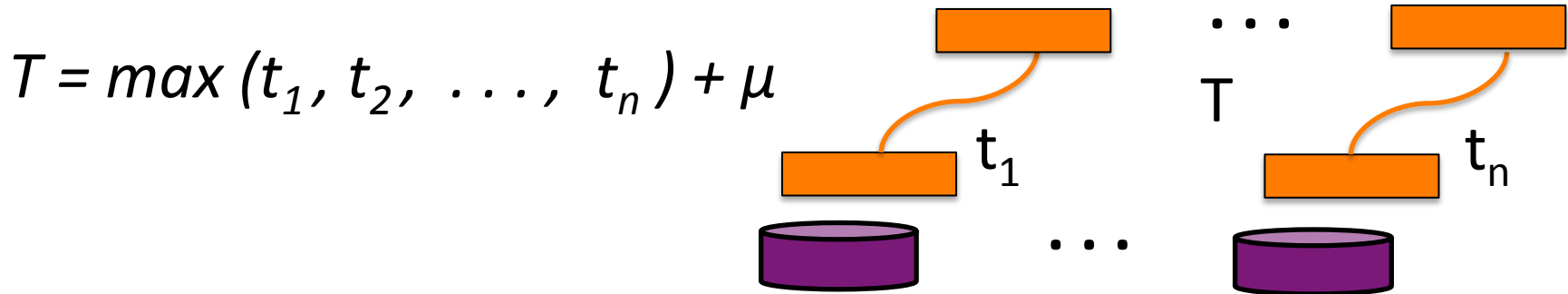
# Modeling Response Time for Parallel I/O

Response time of a single big file request R:

$$T = \max(t_1, t_2, \dots, t_n) + \mu$$



# Simplifying Response Time Model



- Split/merge overhead  $\mu$  is constant
- $n$  small requests  $\approx n$  sampling (**i.i.d.**) of  $n$  IO Servers
- $t_1, \dots, t_n \approx n$  **i.i.d.** statistical variables
- Focus study on one (denoted by  $t$ ) among  $t_1, \dots, t_n$ 
  - $t$ : continuously distributed variable on  $(0, +\infty)$

# Applying Order Statistics to Estimate $T$

$$T = \text{maximum}(t_1, \dots, t_n) + \mu$$

$t$  : continuously distributed variable on  $(0, +\infty)$

$F_t(x)$  : distribution function of  $t$

$f_t(x) = F_t'(x)$  : density function of  $t$

- *Step 1* : Compute density function  $f_{Y_i}(y)$  with  $F_t(x)$  and  $f_t(x)$ 
    - $Y_i$ : the ***i*-th** largest value  $(t_1, t_2, \dots, t_n)$
    - $f_{Y_i}(y) = F(y)^{n-i}(1-F(y))^{n-i} f_t(y) n! / [(i-1)!(n-i)!]$
- } Order Statistics
- *Step 2* : Compute response time  $T = Y_n$

# Problem Statement

- What is the distribution function  $F(t)$  for the response time of each small file request?
  - Existing researches assume
    - Uniform Distribution
    - Normal Distribution
  - Are these assumptions true ?
  - If not, are there other distributions fitting better ?

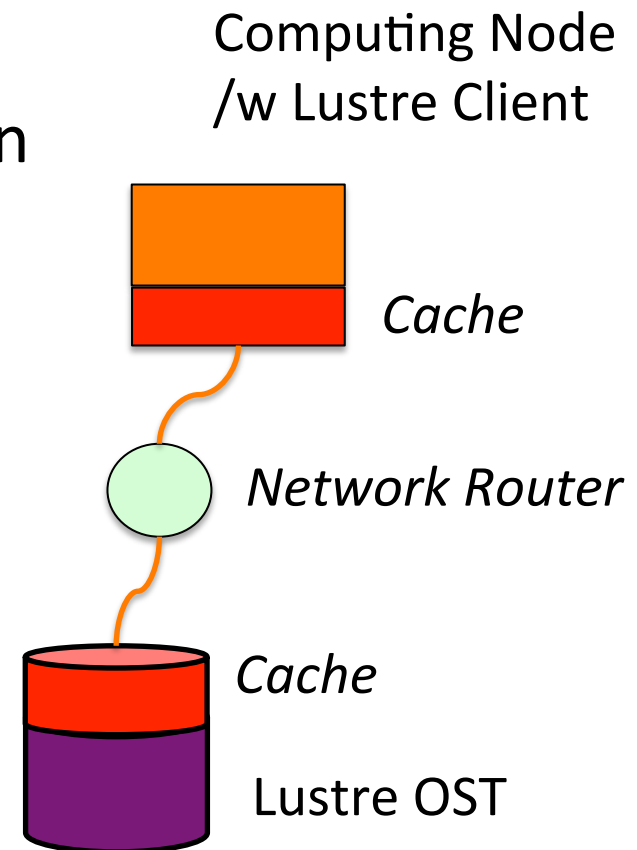
# Our Method

- Sample the response time of two production storage systems
- Analyze statistical properties of response time



# Response Time Sampling Environments

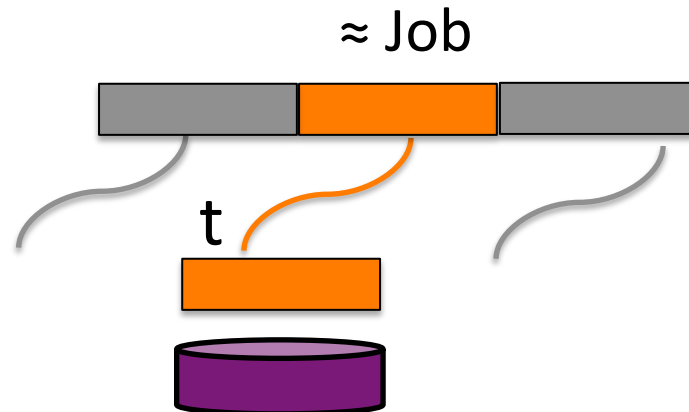
- Hopper and Edison at NERSC<sup>1</sup>
  - *153K and 130K* CPU cores, *1.28 PF* and *2.39PF*
  - *5000* registered users
  - *300* online active users on Edison
  - I/O Intensive jobs use Lustre
- Lustre file system
  - Cache on client and I/O server
  - Network latency
  - 1 ~ 143 OSTes



<sup>1</sup>National Energy Research Scientific Computing Center  
<https://www.nersc.gov/>

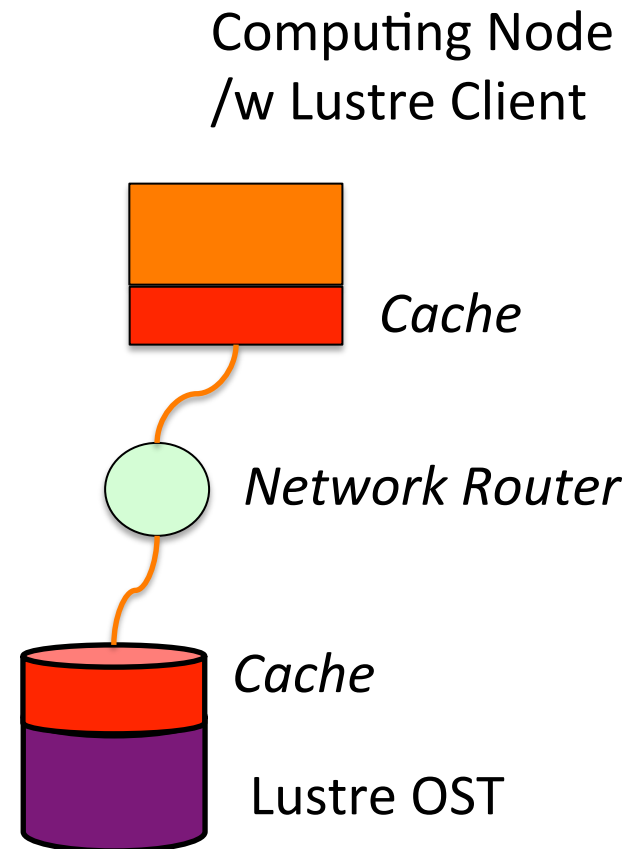
# Sampling Method

- One job sampling one OST
  - A job  $\approx$  A small file request
  - Measure time of reading and writing separately
  - Test different reading/writing sizes
    - 12 different sizes: 512KB, 1MB, 2MB, ... , 1024MB
  - Match request size and striping size



# Sampling Method

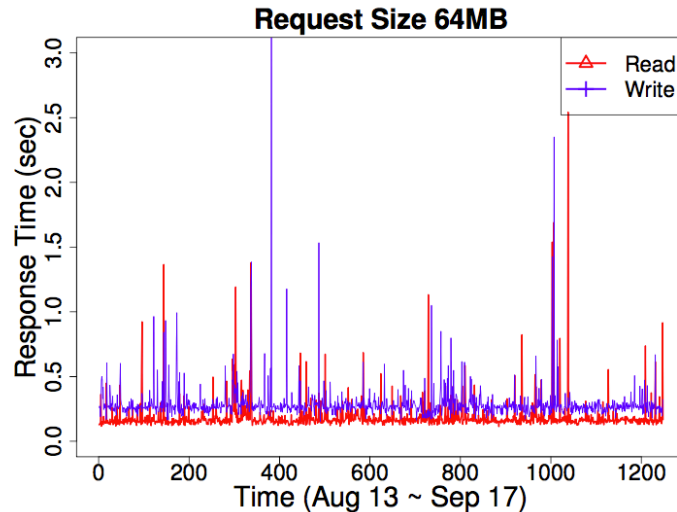
- Measure response time on computing node
  - network, disk, cache
- Cache Consideration
  - No Cache
    - clear cache by accessing memory sized data before sampling
    - call `fsync()` after write
  - Cache
    - High frequently sampling



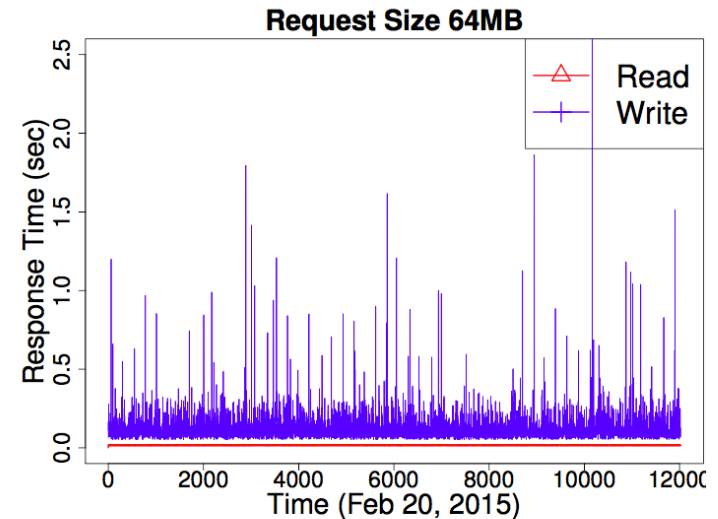
# Sampling Results Statistics Overview

	Start Time	End Time	Days	# of Sampling	# of OSTs
Edison-No-Cache	08/13/2014	09/17/2014	35	14,977	12
Edison-Cache	02/20/2015	02/20/2015	1	927,691	12
Hopper-No-Cache	10/01/2014	01/13/2015	104	13,868	12
Hopper-Cache	02/20/2015	02/20/2015	1	1,581,364	12
	Summary		141	2,537,900	48

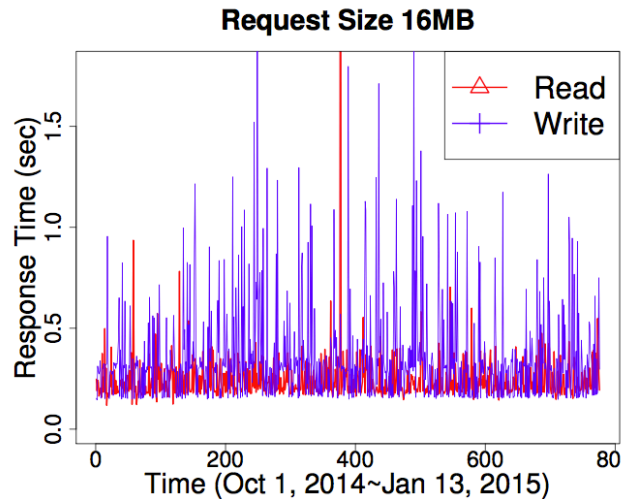
# Variability of Raw Response Time for Edison and Hopper, Cache and No-Cache



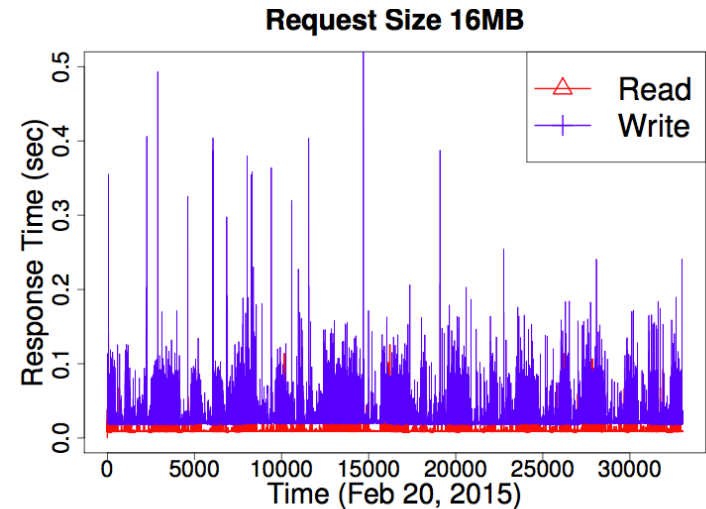
(a) Edison-NoCache



(b) Edison-Cache

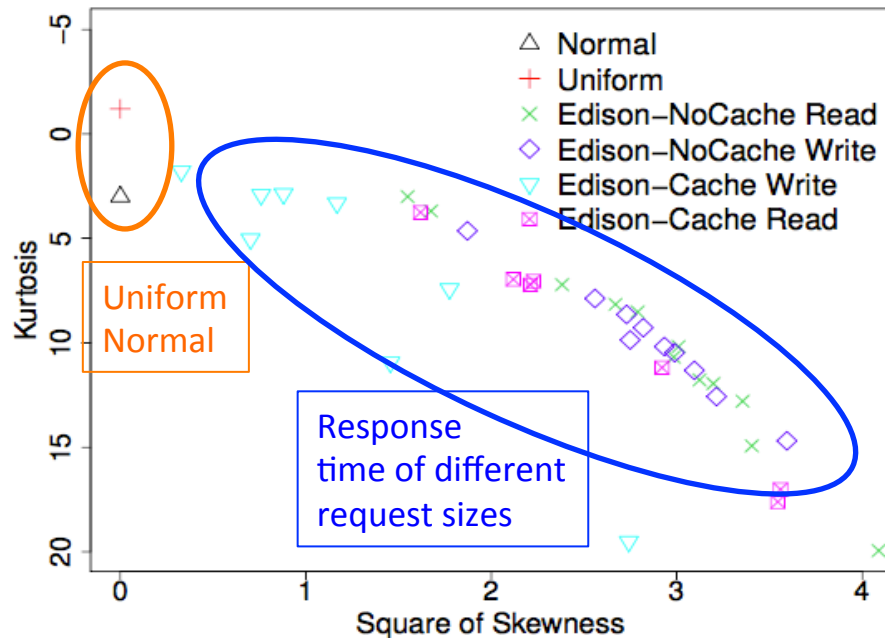


(c) Hopper-NoCache

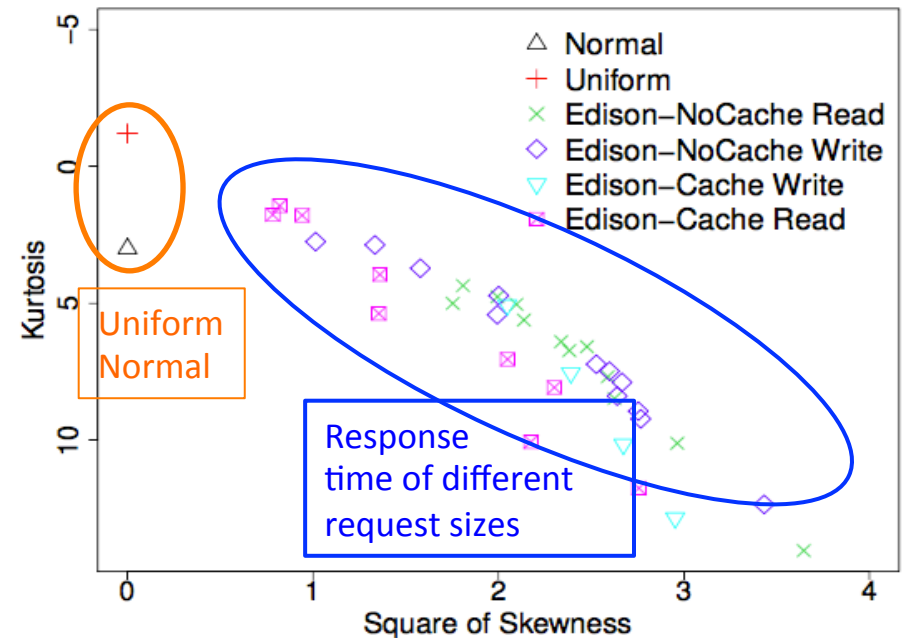


(d) Hopper-Cache

# Ill-fit of Uniform or Normal Distribution



(a) Edison

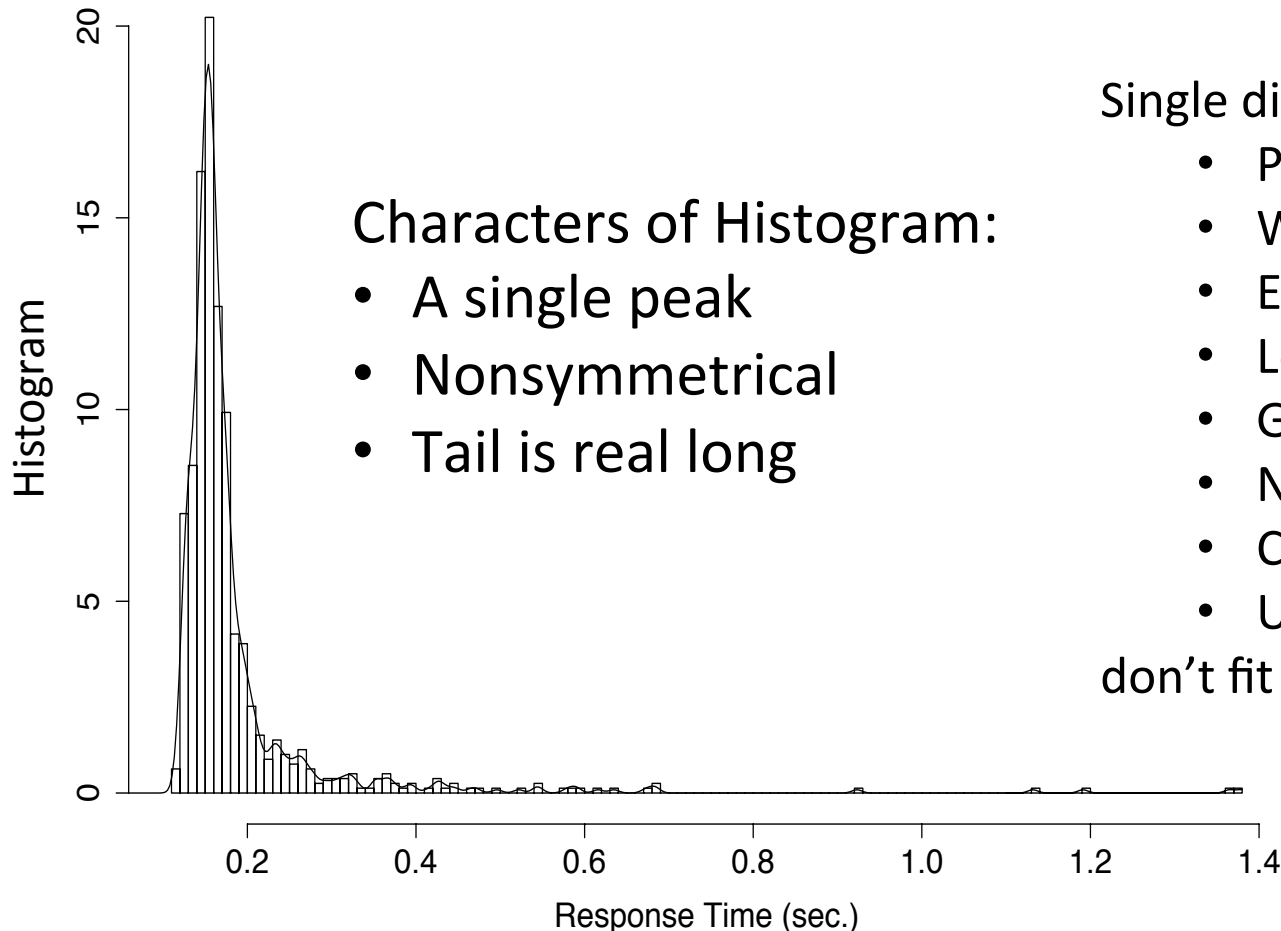


(b) Hopper

Metrics	Uniform	Normal
Kurtosis	- 1.2	3
Skewness	0	0

# Ill-fit of Uniform, Normal, and Other Single Distribution Function

Read (Stripe Size: 64MB)



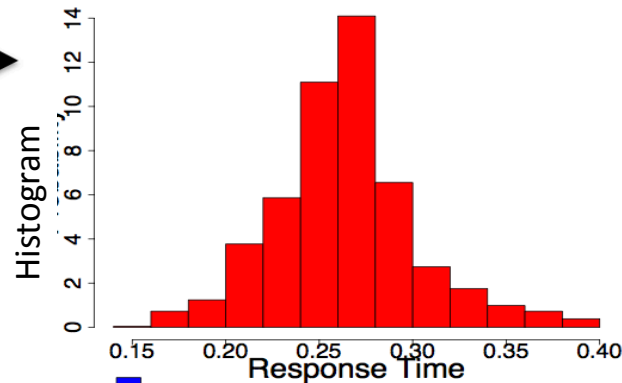
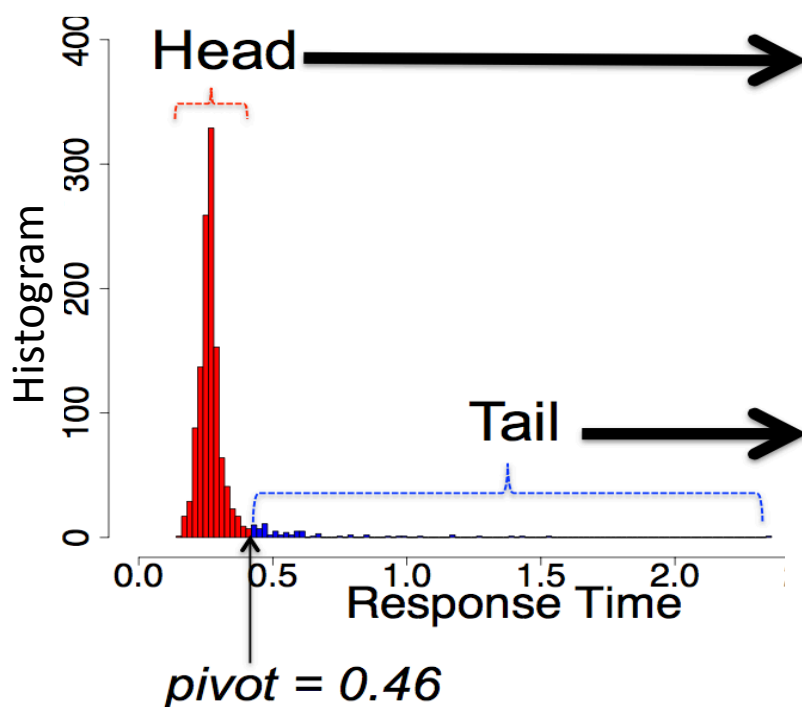
Single distribution functions

- Power Law
- Weibull
- Exponential
- Log Normal
- Gamma
- Normal
- Cauchy
- Uniform

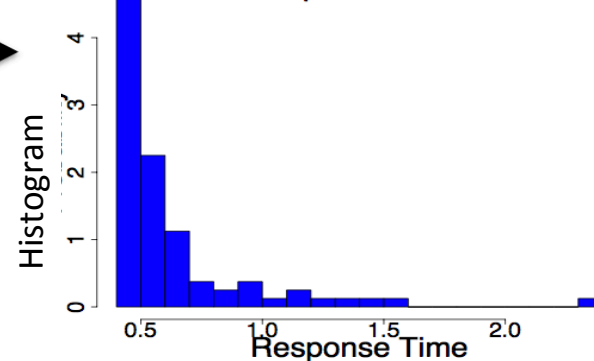
don't fit very well !

# Exploring New Distributions

- Partition response time into Head and Tail
- Find the pivot
  - minimizing KS (Kolmogorov-Smirnov) distances



- Normal
- Cauchy

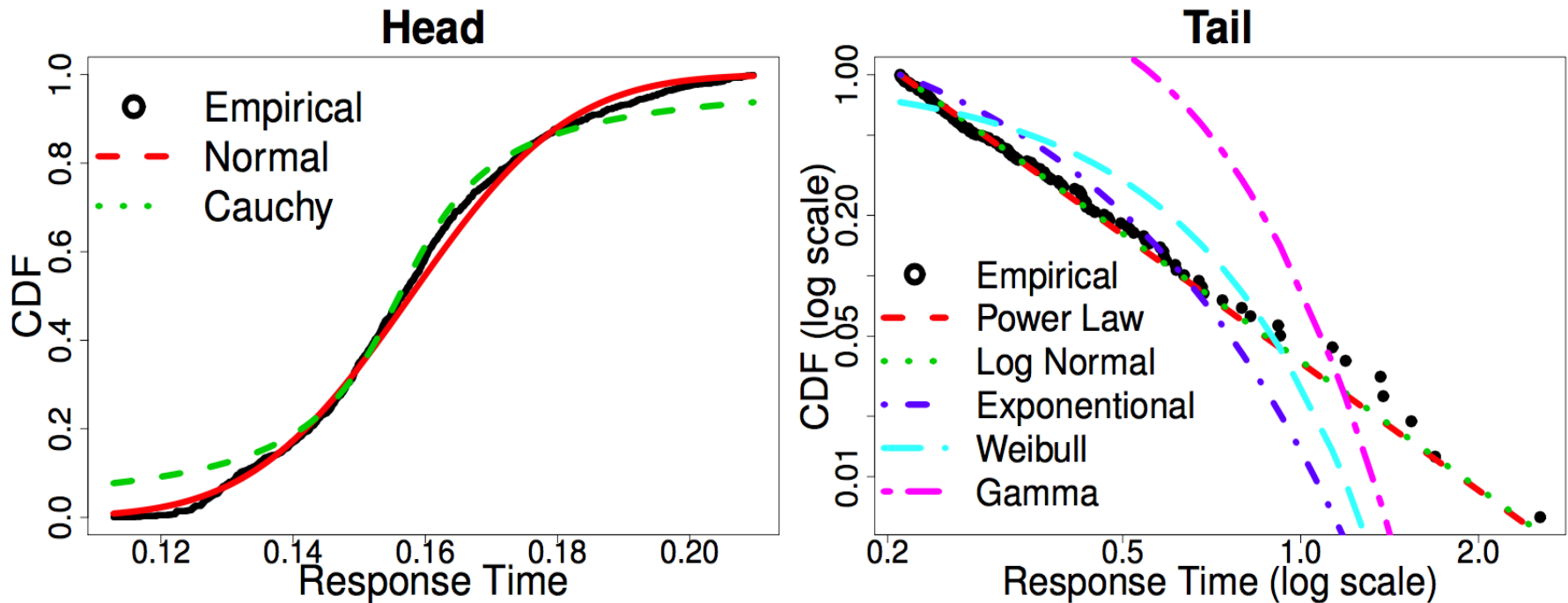


- Power Law
- Weibull
- Exponential
- Log Normal
- Gamma



# Fitting Results

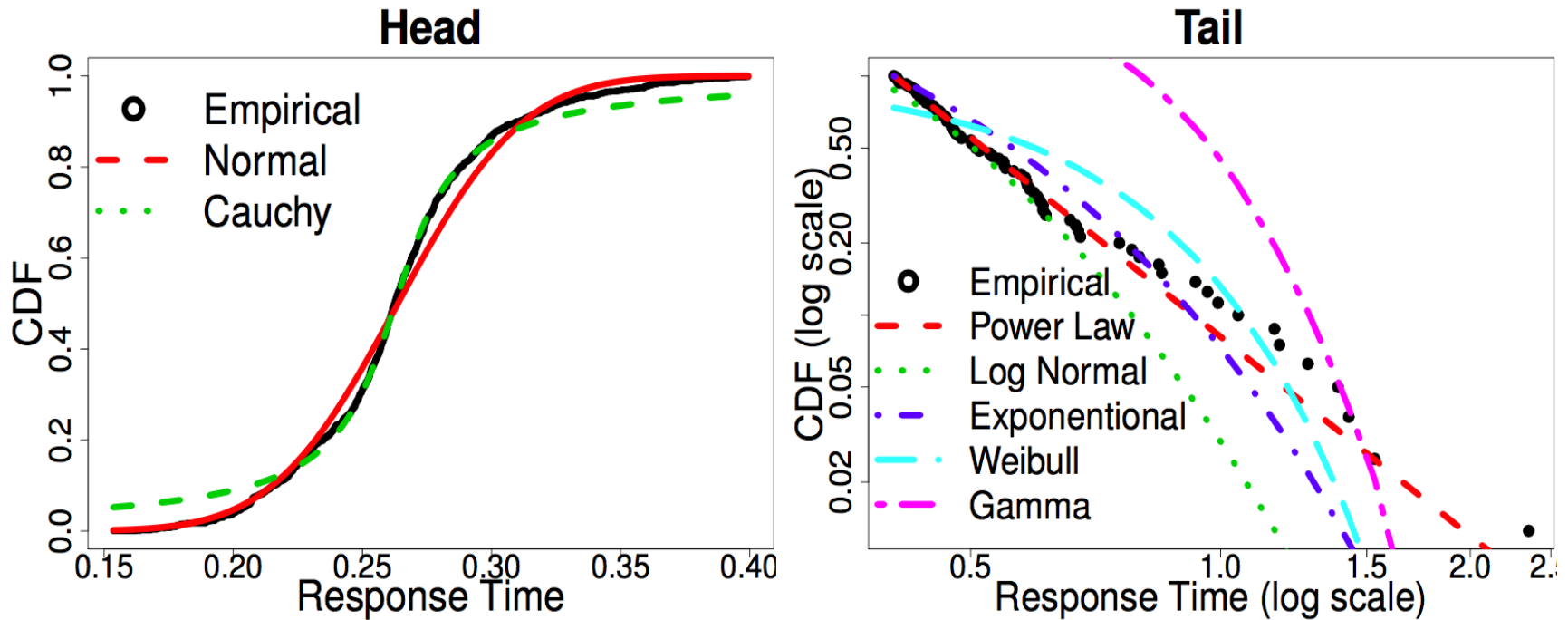
- Edison–NoCache, Read Response Time, 64MB



	Accuracy
Head Group	Normal > Cauchy
Tail Group	Power Law > Log Normal > Exponential > Weibull > Gamma

# Fitting Results

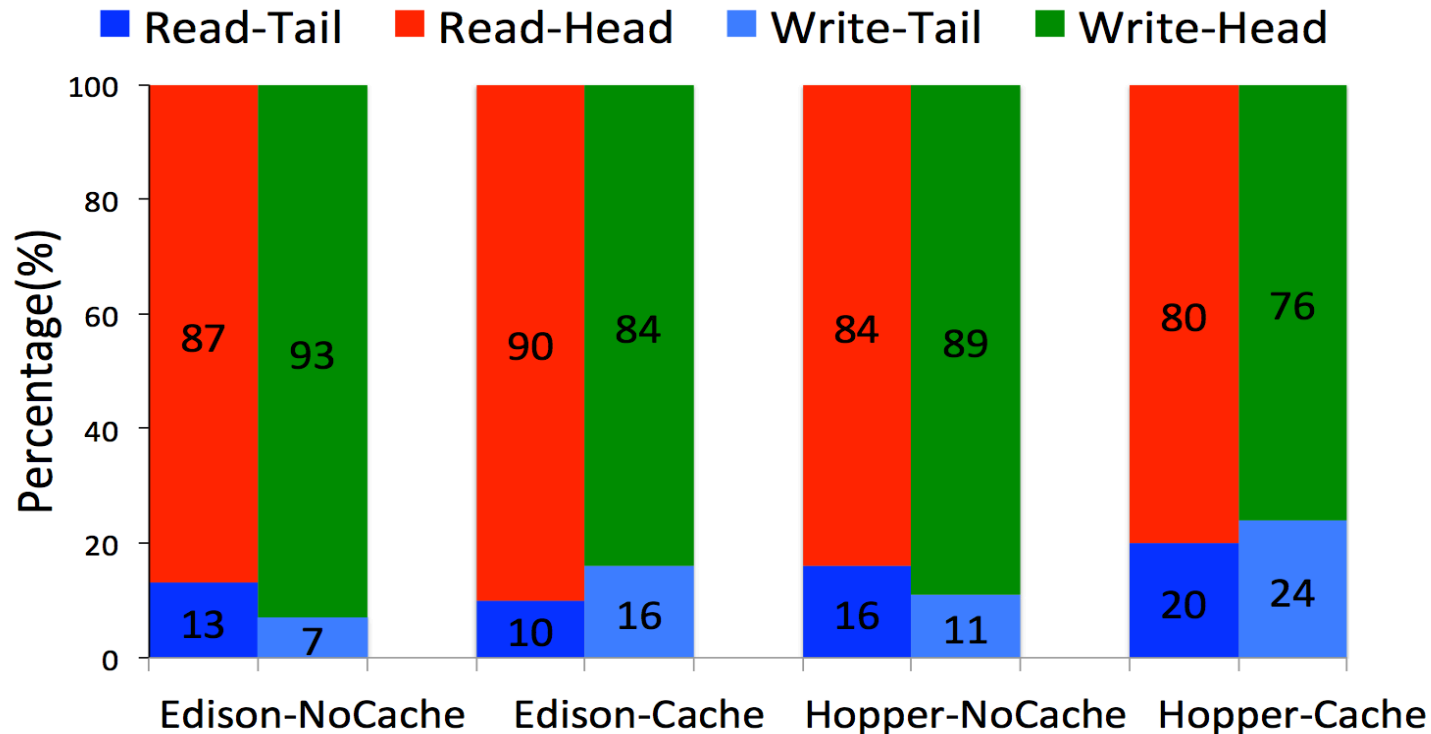
- Edison–NoCache, Write Response Time, 64MB



	Accuracy
Head Group	Normal > Cauchy
Tail Group	Power Law > Weibull > Exponential > Log Normal > Gamma

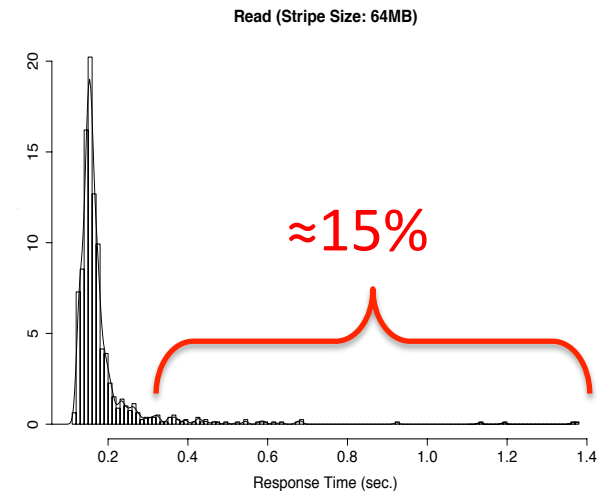
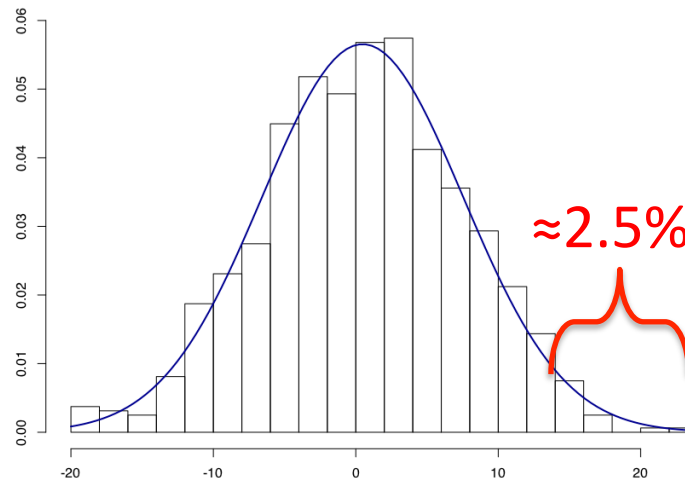
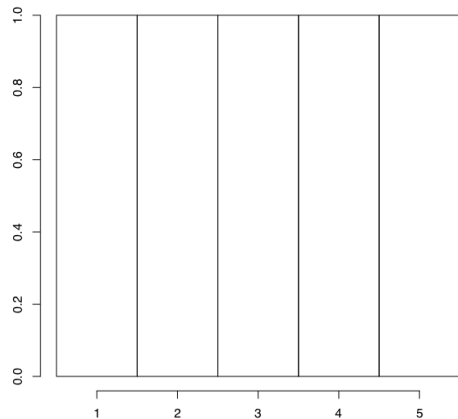
# Percentage of Head group and Tail group

- 85% in Head group (i.e., small response time)
- 15% in Tail group (i.e., long response time)



# What is Wrong with Using Normal or Uniform?

	Long Response Time (Rare Event)
Uniform Distribution	All equal
Normal Distribution	2.5%
Real Storage Systems (Edison and Hopper)	15%



# Summary

- Distribution function of response time of storage system is essential in estimating I/O performance
- We collected *2,537,900* response time sampling from 48 OSTes of 2 petascale storage systems across *141* days
- We found that single Normal or single Power law does not fit the response time
- We found that “Normal + Power law” fits response time better
- Future work
  - sample other storage systems
  - build accurate performance model
  - apply model to applications

# Acknowledgments

- Office of Advanced Scientific Computing Research, Office of Science, U.S. Department of Energy (Program manager: Lucy Nowell), support for the SDS project under contract number DE-AC02-05CH11231



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# Thanks, Questions ?

- other questions, please email to: ***dbin@lbl.gov***

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